## Massachusetts State Learning Standards for Grade Four

| Strand 1: Number Sense and Operations <br> Students engage in problem solving, communicating, reasoning, connecting, and representing as they: | Do you cover/teach this concept/skill? | Do most of your students understand the concept and/or demonstrate competency in the skill? | Do you have adequate resources to teach the concept/skill? | Do you use materials other than those provided to you by Lexington Public Schools? | Understand numbers, ways of representing numbers, relationships among numbers, and number systems <br> $\lambda$ <br> Understand meanings of operations and how they relate to one another <br> $\sigma \quad$ Compute fluently and make reasonable estimates <br> Comments: |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 4.N. 1 Exhibit an understanding of the base ten number system by reading, modeling, writing, and interpreting whole numbers to at least 100,000; demonstrating an understanding of the values of the digits; and comparing and ordering the numbers. |  |  |  |  |  |
| 4.N. 2 Represent, order, and compare large numbers (to at least 100,000 ) using various forms, including expanded notation, e.g., $853=8 \times 100+5 \times 10+3$. : |  |  |  |  |  |
| 4.N. 3 Demonstrate an understanding of fractions as parts of unit wholes, as parts of a collection, and as locations on the number line. : |  |  |  |  |  |
| 4.N. 4 Select, use, and explain models to relate common fractions and mixed numbers ( $1 / 2,1 / 3,1 / 4,1 / 5,1 / 6,1 / 8,1 / 10,1 / 12$, and $1^{1} / 2$ ), find equivalent fractions, mixed numbers, and decimals, and order fractions. : |  |  |  |  |  |
| 4.N. 5 Identify and generate equivalent forms of common decimals and fractions less than one whole (halves, quarters, fifths, and tenths). : |  |  |  |  |  |
| 4.N. 6 Exhibit an understanding of the base ten number system by reading, naming, and writing decimals between 0 and 1 up to the hundredths. |  |  |  |  |  |


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| :---: | :---: | :---: | :---: | :---: | :---: |
| 4.N. 7 Recognize classes (in particular, odds, evens; factors or multiples of a given number; and squares) to which a number may belong, and identify the numbers in those classes. Use these in the solution of problems. : |  |  |  |  |  |
| 4.N. 8 Select, use, and explain various meanings and models of multiplication and division of whole numbers. Understand and use the inverse relationship between the two operations. $\lambda$ |  |  |  |  |  |
| 4.N. 9 Select, use, and explain the commutative, associative, and identity properties of operations on whole numbers in problem situations, e.g., $37 \times 46=46 \times 37$, ( $5 \times 7$ ) $\mathrm{x} 2=5 \times(7 \times 2) . \lambda$ |  |  |  |  |  |
| 4.N. 10 Select and use appropriate operations (addition, subtraction, multiplication, and division) to solve problems, including those involving money. $\lambda$ |  |  |  |  |  |
| 4.N. 11 Know multiplication facts through 12 x 12 and related division facts. Use these facts to solve related multiplication problems and compute related problems, e.g., $3 \times 5$ is related to $30 \times 50,300 \times 5$, and $30 \times 500 . \sigma$ |  |  |  |  |  |
| 4.N. $12{ }^{1}$ Add and subtract (up to five-digit numbers) and multiply (up to three digits by two digits) accurately and efficiently. $\sigma$ |  |  |  |  |  |

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| 4.N. 13 Divide up to a three-digit whole number with a single-digit divisor (with or without remainders) accurately and efficiently. Interpret any remainders. $\sigma$ |  |  |  |  |  |
| 4.N. 14 Demonstrate in the classroom an understanding of and the ability to use the conventional algorithms for addition and subtraction (up to five-digit numbers), and multiplication (up to three digits by two digits). $\sigma$ |  |  |  |  |  |
| 4.N. 15 Demonstrate in the classroom an understanding of and the ability to use the conventional algorithm for division of up to a three-digit whole number with a single-digit divisor (with or without remainders). $\sigma$ |  |  |  |  |  |
| 4.N. 16 Round whole numbers through 100,000 to the nearest $10,100,1000,10,000$, and 100,000. $\sigma$ |  |  |  |  |  |
| 4.N. 17 Select and use a variety of strategies (e.g., front-end, rounding, and regrouping) to estimate quantities, measures, and the results of whole-number computations up to three-digit whole numbers and amounts of money to $\$ 1000$, and to judge the reasonableness of the answer. $\sigma$ |  |  |  |  |  |
| 4. N. 18 Use concrete objects and visual models to add and subtract common fractions. $\sigma$ |  |  |  |  |  |

$\checkmark$ Extend multiplication and division to larger-digit numbers.
$\checkmark$ Use models to explore multiplication and division with fractions (to twelfths) and decimals.
$\checkmark$ Investigate number theory concepts, e.g., prime and composite numbers.
$\checkmark$ Investigate the concept of ratio, e.g., the number of students to the number of teachers.
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Use concrete objects and visual models to add and subtract common decimals.
$\checkmark$ Explore numbers less than zero by extending the number line and by using familiar applications such as temperature.
$\checkmark$ Investigate the distributive property of multiplication over addition for single-digit multipliers, e.g., $7 \times 28$ is equivalent to $7 \times(10+5)$ is equivalent to $7 \times 10+7 \times 5$.

| Strand 2: Patterns, Relations, and Algebra <br> Students engage in problem solving, communicating, reasoning, connecting, and representing as they: | Do you cover/teach this concept/skill? | Do most of your students understand the concept and/or demonstrate competency in the skill? | Do you have adequate resources to teach the concept/skill? | Do you use materials other than those provided to you by Lexington Public Schools? | : Understand patterns, relations, and functions <br> $\lambda$ Represent and analyze mathematical <br> situations and structures using algebraic symbols <br> $\sigma$ Use mathematical models to represent and understand quantitative relationships <br> $v$ Analyze change in various contexts <br> Comments |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 4.P. 1 Create, describe, extend, and explain symbolic (geometric) and numeric patterns, including multiplication patterns like $3,30,300,3000, \ldots$. : |  |  |  |  |  |
| 4.P. 2 Use symbol and letter variables (e.g., $\Delta$, x ) to represent unknowns or quantities that vary in expressions and in equations or inequalities (mathematical sentences that use $=,<,>$ ). $\lambda$ |  |  |  |  |  |
| 4.P.3 Determine values of variables in simple equations, e.g., $4106-\nabla=37,5=\mu+3$, and $\square-\mu=3 . \lambda$ |  |  |  |  |  |
| 4.P. 4 Use pictures, models, tables, charts, graphs, words, number sentences, and mathematical notations to interpret mathematical relationships. $\sigma$ |  |  |  |  |  |
| 4.P. 5 Solve problems involving proportional relationships, including unit pricing (e.g., four apples cost $80 ¢$, so one apple costs 20¢) and map interpretation (e.g., one inch represents five miles, so two inches represent ten miles). $\sigma$ |  |  |  |  |  |
| 4.P. 6 Determine how change in one variable relates to a change in a second variable, e.g., input-output tables. v |  |  |  |  |  |

Exploratory Concepts and Skills
$\checkmark \quad$ Use concrete materials to build an understanding of equality and inequality.
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Appendix \#2
$\checkmark$ Explore properties of equality in number sentences: when equals are added to equals, then the sums are equal; when equals are multiplied by equals, then the products are equal, e.g., if $\square=5$, then $3 \times \square=3 \times 5$.

| Strand 3: Geometry <br> Students engage in problem solving, communicating, reasoning, connecting, and representing as they: | Do you cover/teach this concept/skill? | Do most of your students understand the concept and/or demonstrate competency in the skill? | Do you have adequate resources to teach the concept/skill? | Do you use materials other than those provided to you by Lexington Public Schools? | : Analyze characteristics and properties of two- and three-dimensional geometric shapes and develop mathematical arguments about geometric relationships <br> $\lambda$ Specify locations and describe spatial relationships using coordinate geometry and other representational systems <br> $\sigma$ Apply transformations and use symmetry to analyze mathematical situations <br> $v$ Use visualization, spatial reasoning, and geometric modeling to solve problems <br> Comments: |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 4.G. 1 Compare and analyze attributes and other features (e.g., number of sides, faces, corners, right angles, diagonals, and symmetry) of two- and three-dimensional geometric shapes. : |  |  |  |  |  |
| 4.G. 2 Describe, model, draw, compare, and classify two- and three-dimensional shapes, e.g., circles, polygons-especially triangles and quadrilaterals-cubes, spheres, and pyramids. : |  |  |  |  |  |
| 4.G.3 Recognize similar figures. : |  |  |  |  |  |
| 4.G. 4 Identify angles as acute, right, or obtuse. : |  |  |  |  |  |
| 4.G.5 Describe and draw intersecting, parallel, and perpendicular lines. : |  |  |  |  |  |
| 4.G.6 Using ordered pairs of numbers and/or letters, graph, locate, identify points, and describe paths (first quadrant). $\lambda$ |  |  |  |  |  |
| 4.G. 7 Describe and apply techniques such as reflections (flips), rotations (turns), and translations (slides) for determining if two shapes are congruent. $\sigma$ |  |  |  |  |  |
| 4.G.8 Identify and describe line symmetry in two-dimensional shapes. $\sigma$ |  |  |  |  |  |
| 4.G. 9 Predict and validate the results of partitioning, folding, and combining twoand three-dimensional shapes. $\sigma$ |  |  |  |  |  |

Exploratory Concepts and Skills
$\checkmark$ Predict and describe results of transformations (e.g., translations, rotations, and reflections) on two-dimensional shapes.
$\checkmark$ Investigate two-dimensional representations of three-dimensional objects.
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$\left.\begin{array}{|l|l|l|l|l|l|}\hline \begin{array}{c}\text { Strand 4: Measurement } \\ \text { Students engage in problem solving, } \\ \text { communicating, reasoning, connecting, } \\ \text { and representing as they: }\end{array} & \begin{array}{l}\text { Do you } \\ \text { cover/teach } \\ \text { this } \\ \text { concept/skill? }\end{array} & \begin{array}{l}\text { Do most of } \\ \text { your } \\ \text { students } \\ \text { understand } \\ \text { the concept } \\ \text { and/or } \\ \text { demonstrate } \\ \text { competency } \\ \text { in the skill? }\end{array} & \begin{array}{l}\text { Do you have } \\ \text { adequate } \\ \text { resources to } \\ \text { teach the } \\ \text { concept/skill? }\end{array} & \begin{array}{l}\text { Do you use } \\ \text { materials } \\ \text { other than } \\ \text { those } \\ \text { provided to } \\ \text { you by } \\ \text { Lexington } \\ \text { Public } \\ \text { Schools? }\end{array} & \begin{array}{l}\text { Understand measurable attributes of objects and } \\ \text { the units, systems, and processes of } \\ \text { measurement }\end{array} \\ \hline \text { Apply appropriate techniques, tools, and formulas } \\ \text { to determine measurements }\end{array}\right\}$

Exploratory Concepts and Skills
$\checkmark$ Develop the concepts of area and perimeter by investigating areas and perimeters of regular and irregular shapes created on dot paper, coordinate grids, or geoboards.
$\checkmark$ Use concrete objects to explore volumes and surface areas of rectangular prisms
$\checkmark \quad$ Investigate the use of protractors to measure angles.
$\checkmark$ Identify common measurements of turns, e.g., $360^{\circ}$ in one full turn, $180^{\circ}$ in a half turn, and $90^{\circ}$ in a quarter turn.
$\checkmark$ Investigate areas of right triangles.
$\checkmark$ Understand that measurements are approximations and investigate how differences in units affect precision.

| Strand 5: Data Analysis, Statistics, and Probability <br> Students engage in problem solving, communicating, reasoning, connecting, and representing as they: | Do you cover/teach this concept/skill? | Do most of your students understand the concept and/or demonstrate competency in the skill? | Do you have adequate resources to teach the concept/skill? | Do you use materials other than those provided to you by Lexington Public Schools? | : Formulate questions that can be addressed with data and collect, organize, and display relevant data to answer them <br> $\lambda$ Select and use appropriate statistical methods to analyze data <br> $\sigma$ Develop and evaluate inferences and predictions that are based on data <br> $v$ Understand and apply basic concepts of probability <br> Comments: |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 4.D. 1 Collect and organize data using observations, measurements, surveys, or experiments, and identify appropriate ways to display the data. : |  |  |  |  |  |
| 4.D. 2 Match a representation of a data set such as lists, tables, or graphs (including circle graphs) with the actual set of data. $\lambda$ |  |  |  |  |  |
| 4.D. 3 Construct, draw conclusions, and make predictions from various representations of data sets, including tables, bar graphs, pictographs, line graphs, line plots, and tallies. $\sigma$ |  |  |  |  |  |
| 4.D. 4 Represent the possible outcomes for a simple probability situation, e.g., the probability of drawing a red marble from a bag containing three red marbles and four green marbles. $v$ |  |  |  |  |  |
| 4.D. 5 List and count the number of possible combinations of objects from three sets, e.g., how many different outfits can one make from a set of three shirts, a set of two skirts, and a set of two hats? $v$ |  |  |  |  |  |
| 4.D. 6 Classify outcomes as certain, likely, unlikely, or impossible by designing and conducting experiments using concrete objects such as counters, number cubes, spinners, or coins. $v$ |  |  |  |  |  |

## Exploratory Concepts and Skills

$\checkmark$ Explore the concepts of median, mode, maximum and minimum, and range
$\checkmark$ Discuss what data-collection methods are appropriate for various types of investigations.
$\checkmark$ Explore situations that involve probabilities of equally likely events.
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$\checkmark$ Investigate the construction of simple circle graphs.


[^0]:    ${ }^{1}$ Although this standard is appropriate as stated for this grade span, the state assessment program at the $3-4$ grade span will test multiplication of only up to two digits by two digits at the present time.
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